

Espressioni con le 4 operazioni e le potenze – Con soluzioni

Evaluating Expressions Involving Fractions – With solutions

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1. $\frac{1}{2} + \left(\frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^0 + 1 =$ $\left[\frac{3}{4}\right]$
 2. $1 + \frac{3}{2} - \left(\frac{2}{3}\right)^3 \cdot \left(\frac{2}{3}\right)^2 - \left(\frac{1}{2}\right)^1 =$ $\left[\frac{4}{3}\right]$
 3. $\frac{1}{5} + \left(\frac{2}{3}\right)^2 \cdot \left(\frac{2}{6}\right)^2 - 4 \cdot \left(\frac{17}{4}\right)^0 + \frac{1}{3} =$ $\left[\frac{8}{15}\right]$
 4. $\frac{1}{2} + \left(\frac{2}{3}\right)^6 \cdot \left(\frac{2}{3}\right)^4 - \frac{2}{9} - \frac{2}{3} =$ $\left[\frac{1}{18}\right]$
 5. $\left(\frac{2}{3}\right)^2 - \frac{1}{3} + \left(\frac{1}{3}\right)^3 \cdot \left(\frac{2}{3}\right) \cdot \frac{1}{2} + \left(\frac{1}{3}\right)^0 =$ $\left[\frac{11}{9}\right]$
 6. $\left[\left(\frac{3}{5}\right)^2\right]^4 \div \left(\frac{3}{5}\right)^6 =$ $\left[\frac{9}{25}\right]$
 7. $\left[\left(\frac{2}{7}\right)^2 \cdot \left(\frac{2}{7}\right)^3\right]^2 \div \left(\frac{2}{7}\right)^8 =$ $\left[\frac{4}{49}\right]$
 8. $\left[\left(\frac{2}{3}\right)^4 \cdot \left(\frac{2}{3}\right)^3\right]^2 \div \left(\frac{2}{3}\right)^{12} =$ $\left[\frac{4}{9}\right]$
 9. $\left[\left(\frac{1}{3}\right)^6 \div \left(\frac{1}{3}\right)^4\right]^2 \div \left[\left(\frac{1}{3}\right)^2 \cdot \left(\frac{1}{3}\right)^2\right] =$ $[1]$
 10. $\left[\left(\frac{4}{9}\right)^3 \div \left(\frac{2}{9}\right)^3\right]^2 \div \left[\left(\frac{9}{8}\right)^2 \cdot \left(\frac{16}{9}\right)^2\right]^3 =$ $[1]$
 11. $\left(1 - \frac{1}{2}\right)^4 \div \left\{ \left[\left(\frac{3}{7} + \frac{1}{6} - \frac{5}{14}\right) \cdot \left(5 + \frac{1}{4}\right) - \frac{1}{2} \right]^3 \div \left(\frac{3}{4}\right)^2 - \frac{1}{4} \right\}^3 - \frac{1}{2} =$ $[0]$
 12. $\left\{ 1 - \left[1 - \left(\frac{1}{3} + \frac{1}{6}\right) \right] \right\}^2 \cdot \left[2 - \left(\frac{1}{2} + \frac{7}{10}\right) \div 3 \right]^2 \cdot \left(\frac{3}{4} + \frac{1}{2}\right)^2 =$ $[1]$
 13. $\left(3 - \frac{1}{4}\right) \div \left[\left(\frac{2}{5} + \frac{1}{2} - \frac{5}{6}\right)^2 \cdot \left(\frac{7}{5} + \frac{1}{10} + \frac{7}{2}\right)^2 \right] \div \frac{9}{2} =$ $\left[\frac{11}{2}\right]$
 14. $\left(\frac{1}{2} + \left(\frac{1}{2} + \left(\frac{1}{2} + \frac{2}{6}\right) \cdot \frac{10}{8}\right)\right) \cdot \left(\frac{3}{2}\right)^2 - \left(\frac{1}{2}\right)^4 \cdot \left(\frac{1}{2}\right)^3 =$ $\left[\frac{13}{54}\right]$
 15. $\left[\left(\frac{3}{2} - \frac{3}{4}\right)^3 \cdot \left(\frac{8}{9}\right)^2 + \left(\frac{2}{3} + \frac{1}{2} + \frac{1}{6}\right)^2 \cdot \frac{3}{16} \right] \cdot \left(1 + \frac{1}{2}\right)^2 =$ $\left[\frac{3}{2}\right]$
 16. $\left[\left(\frac{15}{9} - \frac{1}{3}\right)^2 - \left(1 - \frac{1}{3}\right)^2 \div \frac{3}{9} \right] \div \left[\frac{16}{81} \div \frac{16}{27} + \left(\frac{1}{9}\right)^2 \div \frac{2}{30} + \frac{4}{27} \right] =$ $\left[\frac{2}{3}\right]$

17. $\left[\left(\frac{3}{4} \right)^3 \div \left(\frac{3}{4} \right)^2 \div \left(\frac{3}{4} \right) - \left(2 - \frac{2}{3} \right)^2 \div \left(\frac{13}{6} + \frac{1}{2} \right) - \left(\frac{1}{7} - \frac{1}{21} \right) \right] \div \left(\frac{1}{3} + \frac{3}{4} - \frac{13}{84} \right) = \left[\frac{10}{39} \right]$
18. $\left\{ \left[\left(\frac{2}{5} \right)^{10} \div \left(\frac{2}{5} \right)^6 \right]^2 \cdot \left[\left(\frac{2}{5} \right)^8 \div \left(\frac{2}{5} \right)^3 \right] \right\} \div \left[\left(\frac{2}{5} \right)^{10} \cdot \frac{2}{5} \right] = \left[\frac{4}{25} \right]$
19. $\left\{ \left[\left(\frac{1}{3} \right)^4 \cdot \left(\frac{1}{3} \right)^2 \right]^3 : \left(\frac{1}{3} \right)^9 \right\} \div \left[\left(\frac{1}{3} \right)^3 \cdot \frac{1}{3} \right]^2 = \left[\frac{1}{3} \right]$
20. $\left[\left(\frac{3}{4} \right)^6 \div \left(\frac{3}{4} \right)^4 \right]^3 \div \left[\frac{3}{4} \cdot \left(\frac{3}{4} \right)^2 \right]^2 = [1]$
21. $\left\{ \left[\left(1 + \frac{3}{4} - \frac{1}{2} \right)^2 - \left(2 - \frac{7}{4} \right)^2 \right] \div \left(\frac{5}{3} - \frac{1}{6} \right)^3 \right\}^2 \div \left(1 - \frac{5}{9} \right)^2 = [1]$
22. $\left(\frac{2}{3} \right)^2 : \left(\frac{4}{3} \right)^2 + \left(\frac{1}{3} \right)^3 : \left(\frac{1}{3} \right)^2 + \left(\frac{1}{2} \right)^4 : \left(\frac{1}{2} \right)^2 - \left(\frac{2}{3} \right)^5 : \left(\frac{2}{3} \right)^4 + \left(\frac{4}{3} \right)^3 : \left(\frac{4}{3} \right)^3 - \left(\frac{7}{2} \right)^0 = \left[\frac{1}{6} \right]$
23. $\frac{1}{2} + \left\{ \left[\left(1 + \frac{4}{3} \right)^4 \cdot \left(1 - \frac{2}{7} \right)^4 \right]^2 \right\}^6 \div \left\{ \left[\left(3 + \frac{2}{3} \right)^8 \div \left(1 + \frac{1}{2} + \frac{7}{10} \right)^8 \right]^2 \right\}^3 = \left[\frac{3}{2} \right]$
24. $\left\{ \left[\left(\frac{1}{2} \right)^2 \right]^3 \cdot \left[\left(\frac{1}{2} \right)^3 \right]^3 \div \left[\left(\frac{1}{2} \right)^3 \right]^4 \right\}^3 \div \left[\left(\frac{1}{2} \right) \cdot \left(\frac{1}{2} \right)^3 \right]^2 = \left[\frac{1}{2} \right]$
25. $\left\{ \left(\frac{1}{3} \right)^4 \cdot \left(\frac{1}{3} \right)^5 \div \left[\left(\frac{1}{3} \right)^2 \right]^4 \right\}^3 \div \left(\frac{1}{2} \right)^0 = \left[\frac{1}{27} \right]$
26. $\left(1 + \frac{1}{2} \right)^2 \div \frac{5}{4} + \frac{9}{5} \cdot \left(2 - \frac{4}{3} \right)^2 - \left(2 - \frac{3}{5} \right) \cdot \frac{1}{7} - \left(1 - \frac{1}{2} \right)^3 \div \frac{5}{8} = \left[\frac{11}{5} \right]$
27. $\left\{ \left[\left(\frac{7}{9} \right)^{14} \div \left(\frac{7}{9} \right)^{10} \right]^2 \div \left[\left(\frac{7}{9} \right)^3 \cdot \frac{7}{9} \cdot \left(\frac{7}{9} \right)^3 \right] \right\} \div \frac{7}{9} = [1]$
28. $\left\{ \left[\left(\frac{19}{27} + 3 \right) \cdot \frac{16}{5} \right] \div \left[\frac{11}{18} \cdot \left(1 + \frac{31}{33} \right) \right] \right\}^2 \cdot \left(\frac{1}{10} \right)^2 + \left(\frac{1}{2} \right)^4 \div \left(\frac{1}{2} \right)^2 = \left[\frac{3}{4} \right]$
29. $\left\{ \left(\frac{15}{2^4} + \frac{21}{2^5} - 1 \right) \div \left[\frac{3}{2^2} - \left(\frac{1}{2^3} + \frac{1}{2^4} \right) + \frac{5}{2^3 \cdot 3} \right] \right\} \div \frac{95}{74} + 2^2 = \left[\frac{23}{5} \right]$
30. $\left\{ \left[\frac{15}{3} + \frac{3}{8} - \left(\frac{1}{2} \right)^3 - \frac{9}{2} \right] \div \left[\left(\frac{4}{5} \right)^2 + \frac{3}{20} - \left(\frac{1}{5} \right)^2 \right] \right\} - \left[\frac{19}{12} \div \left(\frac{3}{4} + \frac{5}{6} \right) \right] = [0]$
31. $\left[\left(3 + \frac{1}{2} - \frac{5}{3} \right) \cdot \left(\frac{1}{2} \right)^2 \right] \div \left\{ \frac{3}{2} - \left[\frac{2}{3} + \left(\frac{2}{11} + \frac{5}{22} + \frac{7}{33} \right) \div \frac{82}{33} + \frac{1}{12} \right]^5 \right\}^3 \div \frac{1}{4} = \left[\frac{44}{3} \right]$

32. $\left\{ \frac{15}{16} - \left[\left(\frac{3}{2} - \frac{1}{4} \right)^2 \div \frac{5}{4} - \left(\frac{1}{2} + \frac{1}{4} \right)^2 \right] \right\} + \frac{1}{4} = \left[\frac{5}{16} \right]$
33. $\left\{ 1 - \left[1 - \left(\frac{1}{6} + \frac{1}{3} \right) \right] \right\}^2 \cdot \left(\frac{1}{2} + \frac{3}{4} \right)^2 \cdot \left[2 - \frac{1}{3} \cdot \left(\frac{7}{10} + \frac{1}{2} \right) \right]^2 = [1]$
34. $\left\{ \left[\left(\frac{1}{2} + \frac{1}{3} \right)^2 \div \left(1 + \frac{1}{4} \right)^2 \right] + \left[\left(\frac{4}{21} \div \frac{8}{7} + \frac{12}{7} \div \frac{3}{7} \right) \div \left(2 - \frac{7}{6} \right) \right] \right\} \div \left(\frac{7}{3} \right)^2 = [1]$
35. $\left[\frac{1}{3} - \left(\frac{3}{5} - \frac{1}{10} \right)^2 \right] \cdot \frac{3}{5} \div \frac{1}{2} + \frac{7}{4} \div \frac{5}{2} - \frac{2^2}{5} = [0]$
36. $\frac{10}{23} \cdot \left[\left(\frac{2}{7} \div 7 + \frac{5}{49} \right)^2 \div \frac{1}{7} - \left(\frac{1}{2} - \frac{1}{3} \right)^2 \div \frac{5}{6} \right] = \left[\frac{1}{21} \right]$
37. $\left[\left(\frac{5}{8} - \frac{1}{8} \right)^4 - \left(\frac{2}{11} \cdot \frac{22}{3} - 1 \right)^4 \right] \div \left(\frac{1}{4} + \frac{1}{9} \right) \cdot \frac{6}{5} = \left[\frac{1}{6} \right]$
38. $\left[\left(\frac{7}{13} \cdot \frac{26}{21} \right)^3 - \left(\frac{7}{5} \div \frac{14}{5} \right)^3 \right] \div \left[\left(\frac{2}{3} \right)^2 + \frac{2}{3} \div 2 + \frac{1}{4} \right] = \left[\frac{1}{6} \right]$
39. $\left[\left(\frac{1}{2} + \frac{3}{4} - 1 \right)^2 \div \frac{3}{16} + \frac{3}{2} + \left(\frac{1}{4} - \frac{1}{5} \right) \cdot \left(\frac{15}{3} \cdot 2^2 \right) \right] \div \frac{1}{3} = \left[\frac{17}{2} \right]$
40. $\left(1 - \frac{3}{7} \right) \cdot \left[\frac{2}{29} \cdot \left(\frac{11}{5} - \frac{3}{4} \right) + \left(\frac{3}{20} + \frac{4}{15} - \frac{3}{8} \right) : \left(\frac{1}{3} - \frac{1}{4} \right) \right] : \left(\frac{4}{5} \right)^2 + \left(1 - \frac{1}{2} \right)^2 = \left[\frac{9}{16} \right]$
41. $\left[\left(2 + \frac{2}{3} \right) - \left(\frac{1}{3} + \frac{3}{4} - \frac{5}{6} \right) : \left(1 + \frac{1}{2} \right)^2 \right] : \left[\left(1 - \frac{2}{5} \right)^2 \cdot \left(\frac{5}{3} \right)^2 + \frac{7}{2} \cdot \left(\frac{1}{3} \right)^2 \right] = \left[\frac{46}{25} \right]$
42. $\left[\left(\frac{1}{3} \right)^2 \div \left(\frac{1}{6} \right)^2 \right] \cdot \left[\left(\frac{1}{2} \right)^4 \div \left(\frac{1}{15} \div \frac{4}{15} \right) \right] : \left[\left(\frac{3}{2} \right)^2 - \left(1 - \frac{1}{2} \right) \right] = \left[\frac{4}{7} \right]$
43. $\left\{ \left[\left(\frac{1}{6} + \frac{1}{4} \right)^2 \div \left(2 - \frac{1}{3} \right) + \frac{5}{12} - \frac{1}{2} \right] : \left(\frac{1}{4} \right)^2 - \frac{1}{3} \right\} + \frac{1}{4} = \left[\frac{1}{4} \right]$
44. $\left(\frac{1}{3} - \frac{7}{33} \right)^2 : \left(\frac{1}{11} \right)^2 - \left(\frac{11}{9} \right)^4 : \left(\frac{11}{9} \right)^3 = \left[\frac{5}{9} \right]$
45. $\left\{ \left[\left(\frac{5}{3} \right)^2 \cdot \left(1 - \frac{1}{2} \right) \cdot \left(1 + \frac{1}{5} \right)^2 \cdot \left(1 + \frac{1}{2} \right) - \frac{3}{4} \right] : \left(\frac{5}{2} \right)^2 - \left(\frac{1}{5} \right)^2 \right\} : \left[\left(\frac{2}{5} \right)^3 : \left(\frac{2}{5} \right)^2 \right] - \frac{1}{20} = \left[\frac{3}{4} \right]$
46. $\left[\left(1 - \frac{2}{7} \right) \cdot \left(\frac{2}{7} + \frac{19}{7} \right) : \left(1 - \frac{4}{7} \right) + \left(3 - \frac{4}{3} \right)^2 + \left(2 - \frac{1}{2} \right)^2 \right] : \left(3 + \frac{1}{6} \right)^2 + \left(5 - \frac{7}{2} \right)^2 - \left(7 - \frac{13}{2} \right)^2 = [3]$
47. $\left\{ \frac{2}{3} - \left[\left(\frac{1}{2^3} + \frac{1}{2^2} \right) \cdot \frac{2}{3} \right] \right\} \div \left[3 + \left(\frac{1}{3} \right)^4 : \left(\frac{1}{3} \right)^3 \right] + \left[\left(\frac{1}{3} \right)^0 + \left(\frac{1}{3} \right)^5 : \left(\frac{1}{3} \right)^4 \right] \cdot \left(\frac{1}{2} \right)^3 = \left[\frac{7}{24} \right]$

48. $\left(3 - \frac{10}{7}\right) : \left[\left(1 + \frac{1}{2}\right) - \left(1 - \frac{1}{3}\right)^2 \cdot \left(\frac{3}{20} + \frac{6}{35}\right)\right] : 3 =$ [1]
49. $\left[\frac{5^2}{90} \cdot \left(\frac{2}{5}\right)^3 : \left(\frac{2}{5}\right)^2 + \frac{1}{2} \cdot \left(\frac{1}{3}\right)^4 : \left(\frac{1}{3}\right)^3\right] : \left[\left(1 + \frac{2}{3} - \frac{11}{3^2}\right)^2 : \frac{4}{9}\right] =$ $\left[\frac{5}{8}\right]$
50. $\left[\left(\frac{1}{3}\right)^3 : \left(\frac{1}{3}\right)^2 \cdot \left(\frac{1}{3} + \frac{1}{2}\right) : 5 + \left(\frac{1}{9}\right)^4 : \left(\frac{1}{9}\right)^3\right] \cdot \frac{1}{3} + \frac{5}{6} - \left(1 - \frac{2}{3}\right)^2 =$ $\left[\frac{7}{9}\right]$
51. $\left[\left(\frac{1}{2}\right)^2 : \left(\frac{1}{2}\right)^3\right] \cdot \left[\frac{3}{2} - \left(\frac{4}{9}\right)^2 : \left(1 - \frac{5}{9}\right)^2\right] =$ [1]
52. $\left\{\left[\left(\frac{3}{4}\right)^3 \cdot \left(\frac{3}{4}\right)^{2^2}\right]^2 : \left(\frac{3}{4}\right)^8 + \frac{3}{4}\right\} : \frac{7}{4} + \frac{2}{3} =$ $\left[\frac{17}{12}\right]$
53. $\left\{\left[\left(\frac{4}{5}\right)^3 \cdot \left(\frac{4}{5}\right)^{2^2}\right]^2 : \left(\frac{4}{5}\right)^9 + \frac{4}{5}\right\} : \frac{4}{5} - \frac{1}{2} =$ $\left[\frac{3}{2}\right]$
54. $\left\{\left[\left(\frac{2}{3}\right)^3 : \left(\frac{4}{3}\right)^3 + \frac{7}{8} \cdot \left(\frac{1}{4}\right)^0\right]^2 : \left(\frac{7}{8}\right)^1 - \frac{1}{7}\right\} : \frac{4}{5} - \frac{1}{2} =$ $\left[\frac{3}{4}\right]$
55. $\left(\frac{1}{4}\right)^2 : \left(\frac{1}{4}\right)^2 + \left(\frac{1}{2}\right)^2 + \frac{4}{3} - \left(\frac{4}{3}\right)^3 : \left(\frac{4}{3}\right)^2 - \left(\frac{1}{2}\right)^1 =$ $\left[\frac{3}{4}\right]$
56. $\left(\frac{1}{2}\right)^0 + \left[\left(\frac{3}{2} - \frac{1}{4}\right)^2 - \left(1 - \frac{1}{4}\right)^2\right] : \left(\frac{3}{2}\right)^2 - \left(\frac{1}{2}\right)^1 =$ $\left[\frac{17}{18}\right]$
57. $\left(\frac{2}{3} + \frac{2}{6}\right)^1 + \left[\left(\frac{3}{5} - \frac{1}{10}\right)^2 : \left(1 - \frac{1}{3}\right)^2\right] - \left(\frac{1}{2} + \frac{2}{3}\right)^0 - \left(\frac{5}{16}\right)^5 : \left(\frac{5}{16}\right)^4 =$ $\left[\frac{1}{4}\right]$



Soluzioni

$$\begin{aligned}
 & \frac{1}{2} + \left(\frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^0 + 1 = \\
 & = \frac{1}{2} + \frac{1}{4} - 1 + 1 = \\
 & = \frac{1}{2} + \frac{1}{4} = \\
 & = \frac{2+1}{4} = \frac{3}{4}
 \end{aligned}$$

$$\begin{aligned}
 & 1 + \frac{3}{2} - \left(\frac{2}{3}\right)^3 : \left(\frac{2}{3}\right)^2 - \left(\frac{1}{2}\right)^1 = \\
 & = 1 + \frac{3}{2} - \left(\frac{2}{3}\right)^{3-2} - \frac{1}{2} = \\
 & = 1 + \frac{3}{2} - \frac{2}{3} - \frac{1}{2} = \\
 & = \frac{6+9-4-3}{6} = \frac{8}{6} = \frac{4}{3}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{5} + \left(\frac{2}{3}\right)^2 : \left(\frac{2}{6}\right)^2 - 4 \cdot \left(\frac{17}{4}\right)^0 + \frac{1}{3} = \\
 & = \frac{1}{5} + \left(\frac{2}{3} : \frac{2}{6}\right)^2 - 4 \cdot 1 + \frac{1}{3} = \\
 & = \frac{1}{5} + \left(\frac{2}{3} \cdot \frac{6}{2}\right)^2 - 4 + \frac{1}{3} = \\
 & = \frac{1}{5} + \left(\frac{2}{1}\right)^2 - 4 + \frac{1}{3} = \\
 & = \frac{1}{5} + 4 - 4 + \frac{1}{3} = \\
 & = \frac{1}{5} + \frac{1}{3} = \\
 & = \frac{3+5}{15} = \frac{8}{15}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} + \left(\frac{2}{3}\right)^6 : \left(\frac{2}{3}\right)^4 - \frac{2}{9} - \frac{2}{3} = \\
 & = \frac{1}{2} + \left(\frac{2}{3}\right)^{6-4} - \frac{2}{9} - \frac{2}{3} = \\
 & = \frac{1}{2} + \left(\frac{2}{3}\right)^2 - \frac{2}{9} - \frac{2}{3} = \\
 & = \frac{1}{2} + \frac{4}{9} - \frac{2}{9} - \frac{2}{3} = \\
 & = \frac{9+8-4-12}{18} = \frac{1}{18}
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{2}{3}\right)^2 - \frac{1}{3} + \left(\frac{1}{3}\right)^3 : \left(\frac{2}{3}\right) : \frac{1}{2} + \left(\frac{1}{3}\right)^0 = \\
 & = \frac{4}{9} - \frac{1}{3} + \frac{1}{27} \cdot \frac{3}{2} \cdot \frac{2}{1} + 1 = \\
 & = \frac{4}{9} - \frac{1}{3} + \frac{1}{9} + 1 = \\
 & = \frac{4-3+1+9}{9} = \frac{11}{9}
 \end{aligned}$$

$$\begin{aligned}
 & \left[\left(\frac{3}{5}\right)^2\right]^4 \div \left(\frac{3}{5}\right)^6 = \\
 & = \left(\frac{3}{5}\right)^{2 \cdot 4} \div \left(\frac{3}{5}\right)^6 = \\
 & = \left(\frac{3}{5}\right)^8 \div \left(\frac{3}{5}\right)^6 = \\
 & = \left(\frac{3}{5}\right)^{8-6} = \\
 & = \left(\frac{3}{5}\right)^2 = \frac{9}{25}
 \end{aligned}$$

$$\begin{aligned}
 & \left[\left(\frac{2}{7} \right)^2 \cdot \left(\frac{2}{7} \right)^3 \right]^2 \div \left(\frac{2}{7} \right)^8 = \\
 & = \left[\left(\frac{2}{7} \right)^{2+3} \right]^2 \div \left(\frac{2}{7} \right)^8 = \\
 & = \left[\left(\frac{2}{7} \right)^5 \right]^2 \div \left(\frac{2}{7} \right)^8 = \\
 & = \left(\frac{2}{7} \right)^{5 \cdot 2} \div \left(\frac{2}{7} \right)^8 = \\
 & = \left(\frac{2}{7} \right)^{10} \div \left(\frac{2}{7} \right)^8 = \\
 & = \left(\frac{2}{7} \right)^{10-8} = \left(\frac{2}{7} \right)^2 = \frac{4}{49}
 \end{aligned}$$

$$\begin{aligned}
 & \left[\left(\frac{2}{3} \right)^4 \cdot \left(\frac{2}{3} \right)^3 \right]^2 \div \left(\frac{2}{3} \right)^{12} = \\
 & \left[\left(\frac{2}{3} \right)^4 \cdot \left(\frac{2}{3} \right)^3 \right]^2 \div \left(\frac{2}{3} \right)^{12} = \\
 & = \left[\left(\frac{2}{3} \right)^{4+3} \right]^2 \div \left(\frac{2}{3} \right)^{12} = \\
 & = \left[\left(\frac{2}{3} \right)^7 \right]^2 \div \left(\frac{2}{3} \right)^{12} = \\
 & = \left(\frac{2}{3} \right)^{7 \cdot 2} \div \left(\frac{2}{3} \right)^{12} = \\
 & = \left(\frac{2}{3} \right)^{14} \div \left(\frac{2}{3} \right)^{12} = \\
 & = \left(\frac{2}{3} \right)^{14-12} = \left(\frac{2}{3} \right)^2 = \frac{4}{9}
 \end{aligned}$$

$$\begin{aligned}
 & \left[\left(\frac{1}{3} \right)^6 \div \left(\frac{1}{3} \right)^4 \right]^2 \div \left[\left(\frac{1}{3} \right)^2 \cdot \left(\frac{1}{3} \right)^2 \right] = \\
 & \left[\left(\frac{1}{3} \right)^6 \div \left(\frac{1}{3} \right)^4 \right]^2 \div \left[\left(\frac{1}{3} \right)^2 \cdot \left(\frac{1}{3} \right)^2 \right] = \\
 & = \left[\left(\frac{1}{3} \right)^{6-4} \right]^2 \div \left[\left(\frac{1}{3} \right)^{2+2} \right] = \\
 & = \left[\left(\frac{1}{3} \right)^2 \right]^2 \div \left(\frac{1}{3} \right)^4 = \\
 & = \left(\frac{1}{3} \right)^{2 \cdot 2} \div \left(\frac{1}{3} \right)^4 = \\
 & = \left(\frac{1}{3} \right)^4 \div \left(\frac{1}{3} \right)^4 = 1
 \end{aligned}$$

$$\begin{aligned}
 & \left[\left(\frac{4}{9} \right)^3 \div \left(\frac{2}{9} \right)^3 \right]^2 \div \left[\left(\frac{9}{8} \right)^2 \cdot \left(\frac{16}{9} \right)^2 \right]^3 = \\
 & = \left[\left(\frac{4}{9} \div \frac{2}{9} \right)^3 \right]^2 \div \left[\left(\frac{9}{8} \right)^2 \cdot \left(\frac{16}{9} \right)^2 \right]^3 = \\
 & = \left[\left(\frac{4}{\cancel{9}^1} \cdot \frac{\cancel{9}^1}{2} \right)^3 \right]^2 \div \left[\left(\frac{\cancel{9}^1}{8} \cdot \frac{16}{\cancel{9}^1} \right)^2 \right]^3 = \\
 & = \left[(2^3) \right]^2 \div \left[(2^2) \right]^3 = \\
 & = 2^6 \div 2^6 = \\
 & = 2^{6-6} = 2^0 = 1
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 - \frac{1}{2}\right)^4 \div \left\{ \left[\left(\frac{3}{7} + \frac{1}{6} - \frac{5}{14} \right) \cdot \left(5 + \frac{1}{4} \right) - \frac{1}{2} \right]^3 \div \left(\frac{3}{4} \right)^2 - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & \left(1 - \frac{1}{2}\right)^4 \div \left\{ \left[\left(\frac{3}{7} + \frac{1}{6} - \frac{5}{14} \right) \cdot \left(5 + \frac{1}{4} \right) - \frac{1}{2} \right]^3 \div \left(\frac{3}{4} \right)^2 - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & = \frac{1}{16} \div \left\{ \left[\left(\frac{18+7-15}{42} \right) \cdot \frac{21}{4} - \frac{1}{2} \right]^3 \div \frac{9}{16} - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & = \frac{1}{16} \div \left\{ \left[\frac{{}^5 10}{2 \cdot 42} \cdot \frac{21^1}{4_2} - \frac{1}{2} \right]^3 \div \frac{9}{16} - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & = \frac{1}{16} \div \left\{ \left[\frac{3}{4} \right]^3 \div \frac{9}{16} - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & = \frac{1}{16} \div \left\{ \frac{3}{4} - \frac{1}{4} \right\} - \frac{1}{2} = \\
 & = \frac{1}{16} \div \left\{ \frac{1}{2} \right\} - \frac{1}{2} = \\
 & = \frac{1}{2 \cdot 16} \div \frac{1}{8_1} - \frac{1}{2} = \frac{1}{2} - \frac{1}{2} = 0
 \end{aligned}$$

$$\begin{aligned}
 & \left\{ 1 - \left[1 - \left(\frac{1}{3} + \frac{1}{6} \right) \right] \right\}^2 \cdot \left[2 - \left(\frac{1}{2} + \frac{7}{10} \right) \div 3 \right]^2 \cdot \left(\frac{3}{4} + \frac{1}{2} \right)^2 = \\
 & = \left\{ 1 - \left[1 - \frac{2+1}{6} \right] \right\}^2 \cdot \left[2 - \frac{5+7}{10} \div 3 \right]^2 \cdot \left(\frac{3+2}{4} \right)^2 = \\
 & = \left\{ 1 - \left[1 - \frac{3^1}{6_2} \right] \right\}^2 \cdot \left[2 - \frac{12}{10} \cdot \frac{1}{3} \right]^2 \cdot \left(\frac{5}{4} \right)^2 = \\
 & = \left\{ 1 - \left[1 - \frac{3^1}{6_2} \right] \right\}^2 \cdot \left[2 - \frac{{}^2 4 \cdot 12}{10_5} \cdot \frac{1}{3_1} \right]^2 \cdot \frac{25}{16} = \\
 & = \left\{ 1 - \frac{1}{2} \right\}^2 \cdot \left[\frac{10-2}{5} \right]^2 \cdot \frac{25}{16} = \\
 & = \frac{1}{1_4} \cdot \frac{64^{16^1}}{1_25} \cdot \frac{25^1}{16_1} = 1
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 - \frac{1}{4}\right) \div \left[\left(\frac{2}{5} + \frac{1}{2} - \frac{5}{6}\right)^2 \cdot \left(\frac{7}{5} + \frac{1}{10} + \frac{7}{2}\right)^2\right] \div \frac{9}{2} = \\
 & = \left(\frac{12-1}{4}\right) \div \left[\left(\frac{12+15-25}{30}\right)^2 \cdot \left(\frac{14+1+35}{10}\right)^2\right] \div \frac{9}{2} = \\
 & = \frac{11}{4} \div \left[\left(\frac{2^1}{30_{15}}\right)^2 \cdot \left(\frac{50}{10}\right)^2\right] \div \frac{9}{2} = \\
 & = \frac{11}{4} \div \left[\frac{1}{225} \cdot 25\right] \div \frac{9}{2} = \\
 & = \frac{11}{4} \div \frac{1}{9} \div \frac{9}{2} = \\
 & = \frac{11}{4} \cdot \frac{9}{1} \cdot \frac{2}{9} = \frac{11}{2}
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{2} + \left(\frac{1}{2} + \left(\frac{1}{2} + \frac{2}{6}\right) : \frac{10}{8}\right)\right) : \left(\frac{3}{2}\right)^2 - \left(\frac{1}{2}\right)^4 : \left(\frac{1}{2}\right)^3 = \\
 & = \left(\frac{1}{2} + \left(\frac{1}{2} + \left(\frac{1}{2} + \frac{1}{3}\right) \cdot \frac{4}{5}\right)\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{1}{2} + \left(\frac{1}{2} + \frac{5}{3} \cdot \frac{4^2}{5}\right)\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{1}{2} + \left(\frac{1}{2} + \frac{2}{3}\right)\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{1}{2} + \left(\frac{3+4}{6}\right)\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{1}{2} + \frac{7}{6}\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{3+7}{6}\right) \cdot \frac{4}{9} - \frac{1}{2} = \\
 & = \left(\frac{10}{3}\right) \cdot \frac{4^2}{9} - \frac{1}{2} = \\
 & = \frac{20}{27} - \frac{1}{2} = \frac{40-27}{54} = \frac{13}{54}
 \end{aligned}$$